



Wrapping Up: Ch. 3 - Linear programming, Solving Systems of Equations

- 1) Do you feel that there was less homework than the previous unit and did that help you in getting them turned in on time?
- 2) What can you do to improve your learning of the next unit so that you can achieve a better grade?
- 3) How can I (Mr. Hackenberg) help you achieve #2?

<u>HW</u>	<u>Cookies A</u>	<u>Test</u>
0	0/25	85/100
		
30%	70%	

$$0 + \left(\frac{85}{125} \right) \cdot 7$$

$$0 + .476$$

$$= 48\%$$

$$4.2) \textcircled{17}, 30$$

$$4.1) 33, 35$$

$$\textcircled{17} \begin{bmatrix} 2 & 4 \\ 8 & 12 \end{bmatrix} = \begin{bmatrix} 4x-6 & -10t+5x \\ 4x & 15t+1.5x \end{bmatrix}$$

$$4x-6=2$$

$$\quad \quad \quad +6 \quad \quad +6$$

$$\frac{4x}{4} = \frac{8}{4}$$

$$x=2$$

$$\begin{bmatrix} 2 & -10t+5(2) \\ 8 & 15t+1.5(2) \end{bmatrix}$$

$$12 = 15t + 1.5(2)$$

$$12 = 15t + 3$$

$$\quad \quad \quad -3 \quad \quad -3$$

$$9 = 15t$$

$$\frac{9}{15} = \frac{15t}{15}$$

$$\frac{9}{15} = t$$

$$33 \begin{cases} 3x + 2y - 2z = -9 \\ 5x - 3z = -7 \\ x + 4y + 3z = 5 \end{cases}$$

$$\begin{array}{r} 10y - z = -24 \\ -10y - 11z = -24 \\ \hline -12z = -48 \\ \hline z = 4 \end{array}$$

$$\textcircled{1} \quad 3x + 2y - 2z = -9 \quad (5)$$

$$\textcircled{2} \quad 5x - 3z = -7 \quad (-3)$$

$$\begin{array}{r} 15x + 10y - 10z = -45 \\ -15x + 9z = 21 \\ \hline 10y - z = -24 \end{array}$$

$$\textcircled{4} \quad 10y - z = -24$$

$$10y - 4 = -24$$

$$10y = -20$$

$$10y = -20$$

$$\textcircled{y = -2}$$

$$\textcircled{1} \quad 3x + 2y - 2z = -9$$

$$\textcircled{3} \quad x + 4y + 3z = 5 \quad (-3)$$

$$\begin{array}{r} -3x - 12y - 9z = -15 \\ 3x + 2y - 2z = -9 \\ \hline -10y - 11z = -24 \end{array}$$

$$\textcircled{5} \quad -10y - 11z = -24$$

$$\begin{array}{r} 3x + 2(-2) - 2(4) = -9 \\ 3x - 4 - 8 = -9 \\ 3x - 12 = -9 \end{array}$$

$$3x - 12 = -9$$

$$3x = 3$$

$$\textcircled{x = 1}$$

Matrix Multiplication

Scalar Multiplication: $3 \begin{bmatrix} 3 & 5 \\ 2 & 8 \end{bmatrix} = \begin{bmatrix} 9 & 15 \\ 6 & 24 \end{bmatrix}$

~~Ex~~ Solve for: $4x + 2 \begin{bmatrix} 3 & 4 \\ -2 & 1 \end{bmatrix} = \begin{bmatrix} 10 & 0 \\ 4 & 2 \end{bmatrix}$

$$4x + \begin{bmatrix} 6 & 8 \\ -4 & 2 \end{bmatrix} = \begin{bmatrix} 10 & 0 \\ 4 & 2 \end{bmatrix}$$

$$4x = \begin{bmatrix} 10 & 0 \\ 4 & 2 \end{bmatrix} - \begin{bmatrix} 6 & 8 \\ -4 & 2 \end{bmatrix}$$

$$\frac{1}{4} \cdot 4x = \begin{bmatrix} 4 & -8 \\ 8 & 0 \end{bmatrix} \cdot \frac{1}{4}$$

$$x = \begin{bmatrix} 1 & -2 \\ 2 & 0 \end{bmatrix}$$

TRY

$$-3Y + 2 \begin{bmatrix} 6 & 9 \\ -12 & 15 \end{bmatrix} = \begin{bmatrix} 27 & -18 \\ 30 & 6 \end{bmatrix}$$

~~$$\begin{pmatrix} \begin{bmatrix} 5 & -12 \\ 18 & -8 \end{bmatrix} \end{pmatrix}$$~~

$$-3Y + \begin{bmatrix} 12 & 18 \\ -24 & 30 \end{bmatrix} = \begin{bmatrix} 27 & -18 \\ 30 & 6 \end{bmatrix}$$

$$-3Y = \begin{bmatrix} 27 & -18 \\ 30 & 6 \end{bmatrix} - \begin{bmatrix} 12 & 18 \\ -24 & 30 \end{bmatrix}$$

$$\begin{bmatrix} -5 & 12 \\ -18 & 8 \end{bmatrix} \quad -\frac{1}{3} \cdot -3Y = \begin{bmatrix} 15 & -36 \\ 54 & -24 \end{bmatrix}$$

$$Y = \begin{bmatrix} -5 & 12 \\ -18 & 8 \end{bmatrix}$$

CHECK:

$$-3 \begin{bmatrix} -5 & 12 \\ -18 & 8 \end{bmatrix} + 2 \begin{bmatrix} 6 & 9 \\ -12 & 15 \end{bmatrix} = \begin{bmatrix} 27 & -18 \\ 30 & 6 \end{bmatrix}$$

Multiplying 2 matrices

$$A = \begin{bmatrix} -1 & 0 \\ 3 & -4 \end{bmatrix} \quad B = \begin{bmatrix} -3 & 3 \\ 5 & 0 \end{bmatrix}$$

$$AB = \begin{bmatrix} -1(-3) + 0(5) & -1(3) + 0(0) \\ 3(-3) + (-4)(5) & 3(3) + (-4)(0) \end{bmatrix}$$

$$= \begin{bmatrix} 3+0 & -3+0 \\ -9-20 & 9+0 \end{bmatrix}$$

$$AB = \begin{bmatrix} 3 & -3 \\ -29 & 9 \end{bmatrix} \quad BA = \begin{bmatrix} 12 & -12 \\ -5 & 0 \end{bmatrix}$$

$$xy = yx \quad AB \neq BA$$

If A is $m \times n$ and
 B is $n \times p$
 then

AB is $m \times p$

NOTE: column of $A =$ rows of B

↑ if not, can't multiply

$$\begin{matrix} A & & B \\ (2 \times 2) & (2 \times 2) \\ \swarrow & \searrow \\ AB \Rightarrow & 2 \times 2 \end{matrix}$$

$$\begin{matrix} A & & B \\ (4 \times 2) & (2 \times 1) \\ AB = & (4 \times 1) \end{matrix}$$

HW: 4.3 (p. 186)

1, 4, 9, 11, 12

①

20-24, 36

②

14-16, 20-24

- TEST CORRECTIONS
- COOKIE WRITEUP
- EXTENDED PROBLEM

① answer

② why it was wrong.